

**SYM** Construct symbolic numbers, variables and objects.

`S = SYM(A)` constructs an object `S`, of class 'sym', from `A`.

If the input argument is a string, the result is a symbolic number or variable. If the input argument is a numeric scalar or matrix, the result is a symbolic representation of the given numeric values.

`x = sym('x')` creates the symbolic variable with name 'x' and stores the result in `x`. `x = sym('x','real')` also assumes that `x` is real, so that `conj(x)` is equal to `x`. `alpha = sym('alpha')` and `r = sym('Rho','real')` are other examples. Similarly, `k = sym('k','positive')` makes `k` a positive (real) variable. `x = sym('x','unreal')` makes `x` a purely formal variable with no additional properties (i.e., insures that `x` is NEITHER real NOR positive).

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**SYMS** Short-cut for constructing symbolic objects.

`SYMS arg1 arg2 ...`

is short-hand notation for

`arg1 = sym('arg1');`

`arg2 = sym('arg2');` ...

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```
>> syms a s t w x
```

```
>> whos
```

Name	Size	Bytes	Class
a	1x1	126	sym object
ans	1x1	130	sym object
s	1x1	126	sym object
t	1x1	126	sym object
w	1x1	126	sym object
x	1x1	126	sym object

Grand total is 14 elements using 760 bytes

LAPLACE Laplace transform.

$L = \text{LAPLACE}(F)$  is the Laplace transform of the scalar sym  $F$  with default independent variable  $t$ . The default return is a function of  $s$ . If  $F = F(s)$ , then LAPLACE returns a function of  $t$ :  $L = L(t)$ . By definition  $L(s) = \int_0^{\infty} (F(t) \cdot \exp(-s \cdot t)) dt$ , where integration occurs with respect to  $t$ .

$L = \text{LAPLACE}(F, t)$  makes  $L$  a function of  $t$  instead of the default  $s$ :  
 $\text{LAPLACE}(F, t) \Leftrightarrow L(t) = \int_0^{\infty} (F(x) \cdot \exp(-t \cdot x)) dx$ .

$L = \text{LAPLACE}(F, w, z)$  makes  $L$  a function of  $z$  instead of the default  $s$  (integration with respect to  $w$ ).

$\text{LAPLACE}(F, w, z) \Leftrightarrow L(z) = \int_0^{\infty} (F(w) \cdot \exp(-z \cdot w)) dw$ .

Examples:

```
syms a s t w x
laplace(t^5)      returns 120/s^6
laplace(exp(a*s)) returns 1/(t-a)
laplace(sin(w*x),t) returns w/(t^2+w^2)
laplace(cos(x*w),w,t) returns t/(t^2+x^2)
laplace(x^sym(3/2),t) returns 3/4*pi^(1/2)/t^(5/2)
laplace(diff(sym('F(t)'))) returns laplace(F(t),t,s)*s-F(0)
```

---

```
>> syms a s t w x
>> laplace(t^5)
```

```
ans =
```

```
120/s^6
```

```
>> pretty(ans)
```

```
      120
      ---
       6
      s
```

ILAPLACE Inverse Laplace transform.

$F = \text{ILAPLACE}(L)$  is the inverse Laplace transform of the scalar sym  $L$  with default independent variable  $s$ . The default return is a function of  $t$ . If  $L = L(t)$ , then  $\text{ILAPLACE}$  returns a function of  $x$ :

$F = F(x)$ .

By definition,  $F(t) = \int_{c-i\infty}^{c+i\infty} L(s) \exp(s*t) ds$  where  $c$  is a real number selected so that all singularities of  $L(s)$  are to the left of the line  $s = c$ ,  $i = \sqrt{-1}$ , and the integration is taken with respect to  $s$ .

$F = \text{ILAPLACE}(L,y)$  makes  $F$  a function of  $y$  instead of the default  $t$ :

$\text{ILAPLACE}(L,y) \Leftrightarrow F(y) = \int_{c-i\infty}^{c+i\infty} L(y) \exp(s*y) ds$ .

Here  $y$  is a scalar sym.

$F = \text{ILAPLACE}(L,y,x)$  makes  $F$  a function of  $x$  instead of the default  $t$ :

$\text{ILAPLACE}(L,y,x) \Leftrightarrow F(y) = \int_{c-i\infty}^{c+i\infty} L(y) \exp(x*y) dy$ , integration is taken with respect to  $y$ .

Examples:

```
syms s t w x y
ilaplace(1/(s-1))      returns exp(t)
ilaplace(1/(t^2+1))    returns sin(x)
ilaplace(t^(-sym(5/2)),x) returns 4/3/pi^(1/2)*x^(3/2)
ilaplace(y/(y^2 + w^2),y,x) returns cos(w*x)
ilaplace(sym('laplace(F(x),x,s)'),s,x) returns F(x)
```

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>> ilaplace(1/(s-1))

ans =

exp(t)