

**SUMMARY OF EFFORT AND FLOW RELATIONSHIPS**  
ENBE 471

**Power Variables**

Energy Domain	Effort (e) (Generally expressed as a gradient)	Flow (f)
Electrical	Voltage ( $v$ )	Current ( $i$ )
Rotational Mechanics	Torque ( $\tau$ )	Angular Velocity ( $\omega$ )
Translational Mechanics	Force ( $F$ )	Velocity ( $v$ )
Hydraulic Circuits	Pressure ( $P$ )	Volume Flow Rate ( $Q$ )
Thermal	Temperature ( $T$ )	Entropy Flow Rate ( $S$ )
Chemical Diffusion	Chemical Potential ( $\mu$ )	Molar Flow Rate ( $n$ )

**Some Useful Alternate Units**

Thermal	Temperature ( $T$ )	Heat Flow Rate ( $q$ )
Diffusion	Concentration ( $C$ )	Molar or Mass Flow Rate ( $n$ )

**Storage Elements** (accumulate either effort or flow)

Energy Domain	$\int$ effort (Momentum)	$\int$ flow (Displacement)
General Formula	$\int_0^t e \, dt$	$\int_0^t f \, dt$
Rotational Mechanics	Angular Momentum ( $h$ )	Angular Displacement ( $\omega$ )
Translational Mechanics	Momentum ( $P$ )	Displacement ( $y$ )
Hydraulics	Pressure Momentum ( $\gamma$ )	Volume ( $V$ )
Thermal	—	Entropy ( $S$ ) – Power Energy ( $H$ ) – Alternate
Chemical	—	Moles ( $n$ )

## Elements

Element	Effort	Flow	Relation Type
<i>Resistance</i> e.g. Resistance, Damping Factor Fluid Resistance Thermal Resistance	$e = e(f)$	$f = f(e)$	Nonlinear
	$e = Rf$	$f = \frac{e}{R} = Ge$	Linear
<i>Capacitance</i> (Integrated Flow Element)  e.g. Capacitance Thermal Capacitance Fluid Capacitance Spring Constant Compliance	$e = e(q)$ or $e = e\left(\int_0^t f dt\right)$	$f = \frac{dq}{dt}$ or $f = \frac{dq(e)}{dt}$	Nonlinear
	$e = \frac{q}{C}$ or $e = \frac{\int_0^t f dt}{C}$	$f = \frac{dq}{dt}$ or $f = \frac{dCe}{dt}$ or $f = C \frac{de}{dt}$	Linear
<i>Inertance</i> (Integrated Effort Element)  p = momentum I = Inertance Inductance Fluid Inertia	$e = \frac{dp}{dt}$	$f = f(p)$	Nonlinear
	or	or	
	$e = \frac{dp(f)}{dt}$	$f = f\left(\int_0^t e dt\right)$	
	or	$f = \frac{p}{I}$	Linear
	$e = \frac{dp}{dt}$	or	
	or	$f = \frac{\int_0^t e dt}{I}$	
or	$e = \frac{df}{dt}$		
or	$e = I \frac{df}{dt}$		
or	$e = I \ddot{q}$		

### Connectors

Element	Effort	Flow	Relation Type
<i>Transformer</i> m = modulus of the transformer	$e_1 = m(e_2)$	$f_2 = m(f_1)$	Nonlinear
	$e_1 = m e_2$	$f_2 = m f_1$	Linear
<i>Gyrator</i> r = modulus of the gyrator	or $e_1 = r(f_2)$ $e_2 = r(f_1)$	or $f_1 = \frac{1}{r}(e_2)$ $f_2 = \frac{1}{r}(e_1)$	Nonlinear
	or $e_1 = r f_2$ $e_2 = r f_1$	or $f_1 = \frac{e_2}{r}$ $f_2 = \frac{e_1}{r}$	Linear
<i>Common Effort Junction</i>	$e_1 = e_2 = e_3 = e_4 = \dots$	$\sum f = 0$	
<i>Common Flow Junction</i>	$\sum e = 0$	$f_1 = f_2 = f_3 = f_4 = \dots$	